Understanding the 2020 Census Disclosure Avoidance System:

Analysis of Production Settings for Redistricting and Voting Rights Act Use Cases

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We also acknowledge and greatly appreciate the ongoing feedback we have received from external stakeholder groups that has contributed to the design and improvement of the Disclosure Avoidance System.

For more information and technical details relating to the issues discussed in these slides, please contact the author at michael.b.hawes@census.gov.

Any opinions and viewpoints expressed in this presentation are the author's own, and do not represent the opinions or viewpoints of the U.S. Census Bureau.



Production Settings for 2020 Census P.L 94-171 Redistricting Data Summary File

FOR IMMEDIATE RELEASE: WEDNESDAY, JUNE 09, 2021

Census Bureau Sets Key Parameters to Protect Privacy in 2020 Census Results

JUNE 09, 2021 RELEASE NUMBER CB21-CN.42









JUNE 9, 2021 — The U.S. Census Bureau's Data Stewardship Executive Policy Committee (DSEP) announced it has selected the settings and parameters for the Disclosure Avoidance System (DAS) for the 2020 Census redistricting data (PL-94-171). The DAS uses a mathematical algorithm to ensure that the privacy of





Stakeholder Feedback

We received a substantial amount of invaluable feedback on the April 2021 Demonstration Data.

Major themes included:

- Accuracy for American Indian and Alaska Native tribal areas and other "off-spine" geographies
- Accuracy for places, Minor Civil Divisions, and tract-level data
- Bias (geographic and characteristic)
- Race and Ethnicity statistics
- Occupancy rates





Key Parameters and Improvements

Privacy-loss Budget (PLB):
 ε= 17.14 for persons

 ε = 2.47 for units

- Improvements to the optimized geographic post-processing hierarchy
- Extra PLB allocated to Population counts
- Extra PLB allocated to Race and Ethnicity statistics
- Extra PLB allocated to occupancy rates at the block-group level and above



Privacy-loss Budget Allocations

https://www2.census.gov/programs-surveys/decennial/2020/program-management/data-product-planning/2010-demonstration-data-products/ProductionSettings20210608/2021-06-08-privacy-loss_budgetallocation.pdf





Privacy-loss Budget Allocations by geographic level

April 2021 Demonstration Data:

Global rho		1.05
Global epsilon		10.3
delta		10-10
	cation by phic Level	
US	51/1024	
State	153/1024	
County	78/1024	
Tract	51/1024	
Optimized Block Group*	172/1024	
Block	519/1024	

Production Settings:

Global rho		2.56
Global epsilon		17.14
delta		10-10
	cation by phic Level	
US	104/4099	
State	1440/4099	
County	447/4099	
Tract	687/4099	
Optimized Block Group*	1256/4099	
Block	165/4099	



Privacy-loss Budget Allocations by query

April 2021 Demonstration Data:

	Per Query rho Allocation by Geographic Level					
Query	US	State	County	Tract	Optimized Block Group*	Block
TOTAL (1 cell)		678/1024**	342/1024	1/1024	572/1024	1/1024
CENRACE (63 cells)	2/1024	1/1024	1/1024	2/1024	1/1024	2/1024
HISPANIC (2 cells)	1/1024	1/1024	1/1024	1/1024	1/1024	1/1024
VOTINGAGE (2 cells)	1/1024	1/1024	1/1024	1/1024	1/1024	1/1024
HHINSTLEVELS (3 cells)	1/1024	1/1024	1/1024	1/1024	1/1024	1/1024
HHGQ (8 cells)	1/1024	1/1024	1/1024	1/1024	1/1024	1/1024
HISPANIC*CENRACE (126 cells)	5/1024	2/1024	3/1024	5/1024	3/1024	5/1024
VOTINGAGE*CENRACE (126 cells)	5/1024	2/1024	3/1024	5/1024	3/1024	5/1024
VOTINGAGE*HISPANIC (4 cells)	1/1024	1/1024	1/1024	1/1024	1/1024	1/1024
VOTINGAGE*HISPANIC*CENRACE (252 cells)	17/1024	6/1024	11/1024	17/1024	8/1024	17/1024
HHGQ*VOTINGAGE* HISPANIC*CENRACE (2,016 cells)	990/1024	·		989/1024	432/1024	989/1024

Production Settings:

	Per Query rho Allocation by Geographic Level						
Query	US	State	County	Tract	Optimized Block Group*	Block	
TOTAL (1 cell)		3773/4097**	3126/4097	1567/4102	1705/4099	5/4097	
CENRACE (63 cells)	52/4097	6/4097	10/4097	4/2051	3/4099	9/4097	
HISPANIC (2 cells)	26/4097	6/4097	10/4097	5/4102	3/4099	5/4097	
VOTINGAGE (2 cells)	26/4097	6/4097	10/4097	5/4102	3/4099	5/4097	
HHINSTLEVELS (3 cells)	26/4097	6/4097	10/4097	5/4102	3/4099	5/4097	
HHGQ (8 cells)	26/4097	6/4097	10/4097	5/4102	3/4099	5/4097	
HISPANIC*CENRACE (126 cells)	130/4097	12/4097	28/4097	1933/4102	1055/4099	21/4097	
VOTINGAGE*CENRACE (126 cells)	130/4097	12/4097	28/4097	10/2051	9/4099	21/4097	
VOTINGAGE*HISPANIC (4 cells)	26/4097	6/4097	10/4097	5/4102	3/4099	5/4097	
VOTINGAGE*HISPANIC*CENRACE (25 2 cells)	26/241	2/241	101/4097	67/4102	24/4099	71/4097	
HHGQ*VOTINGAGE* HISPANIC*CENRACE (2,016 cells)	189/241	230/4097	754/4097	241/2051	1288/4099	3945/4097	

^{*}The Optimized Block Groups used within the TopDown Algorithm differ from tabulation block groups. These differences improve accuracy for "off-spine" geographies like places and minor civil divisions. The use of optimized block groups for measurement and post-processing within the TopDown Algorithm does not impact how the resulting data will be tabulated. All Census data products will be tabulated using the official tabulation block groups as defined by the Census Bureau's Geography Division.





^{**}The TOTAL query (total population) is held invariant at the state level. This rho allocation assigned to TOTAL at the state level is the amount assigned to the state-level queries for the total population of all American Indian and Alaska Native (AIAN) tribal areas within the state and for the total population of the remainder of the state, for the 36 states that include AIAN tribal areas.

Public Release of the 2020 Census P.L. 94-171 Redistricting Data Summary Files

The Census Bureau will release these data on its public FTP site on August 12, 2021.

The Census Bureau will release the same data in easier-to-use formats by September 30, 2021.

For more information, visit the Census Bureau's website at <u>www.census.gov</u>.





Production Settings 2010 Demonstration Data Release

In parallel with the release of the 2020 Census P.L. 94-171 Redistricting Data Summary Files, the Census Bureau will also be releasing the final set of 2010 Census Demonstration Data reflecting the final production settings used by the 2020 Census Disclosure Avoidance System to protect the 2020 Census redistricting data.

These are the same data used to produce the Production Settings Detailed Summary Metrics released on July 1, 2021.

https://www.census.gov/programs-surveys/decennialcensus/decade/2020/planning-management/process/disclosureavoidance/2020-das-development.html





Analyses of 2010 Census Demonstration Data for Redistricting and Voting Rights Act Use Cases

 Empirical Study of Two Aspects of the Topdown Algorithm Output for Redistricting: Reliability & Variability

Updated version of Wright and Irimata (2021) study.

 Analysis of the impact of DAS production settings on the identification of majorityminority districts



Comparisons to Published 2010 Census Data

Both sets of analyses discussed today involve comparisons of the 2010 Census Demonstration Data (protected with the differentially private 2020 Census Disclosure Avoidance System) to published 2010 Census tabulations.

The 2010 Census used a form of noise infusion known as data swapping, wherein households' records were swapped across geographies to protect the confidentiality of individuals' census responses.

For the 2010 Census, the number of individuals and the number of voting-age individuals in each household were held invariant (no noise was added), but individuals' characteristics (e.g., race and Hispanic origin) were swapped across geographies.

Differences between the Demonstration Data and the published 2010 Census tabulations presented in the following analyses reflect both the noise from the 2020 Census Disclosure Avoidance System and impact of the 2010 Census swapping methodology on characteristics data.



Average Error in Total Population Counts by Geographic Level

Geographic Level	Mean Absolute Error (MAE) (# of persons)
Counties	1.75
Minor Civil Divisions (MCD)	2.74
Incorporated Places	3.55
Tracts	1.93
Blocks (Urban blocks)	4.22
Blocks (Rural blocks)	1.61

Source: <u>Production Settings Detailed Summary Metrics</u>

CBDRB-FY20-DSEP-001



EMPIRICAL STUDY OF TWO ASPECTS OF THE TOPDOWN ALGORITHM OUTPUT FOR REDISTRICTING: RELIABILITY & VARIABILITY

(August 5, 2021 Update)

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Available at: https://www.census.gov/library/working- papers/2021/adrm/SSS2021-02.html



Research Questions:

(1) What is the minimum TOTAL population of a district to have reliable characteristics of various demographic groups for redistricting purposes?

Because districts cannot be defined ex ante, this portion of their analysis uses two existing geographic levels as proxies for districts:

- Block Groups ("on spine")
- Places and Minor Civil Divisions ("off spine")
- (2) How variable are data protected using the 2020 Disclosure Avoidance System for districts in Rhode Island and for three additional jurisdictions?

Part 1: Reliability of demographic characteristics

Definition 1: Let $C_{SWA}(g)$ and $C_{TDA}(g)$ be two competing counts of the demographic group g associated with a block group (more generally, geographic district) whose total population counts are C_{SWA} and C_{TDA} , respectively. The **difference of ratios** is the absolute value of the difference between the SWA ratio $\frac{C_{SWA}(g)}{C_{SWA}}$ and the TDA ratio $\frac{C_{TDA}(g)}{C_{TDA}}$, given by:

$$DR_g = \left| \frac{C_{SWA}(g)}{C_{SWA}} - \frac{C_{TDA}(g)}{C_{TDA}} \right|. \tag{1}$$

Small values of the difference of ratios DR_g imply that the ratios for a group g due to SWA and TDA in the block group, MCD, or place are close.

Definition 2: When DR_g is sufficiently small while comparing a $C_{SWA}(g)$ count and corresponding $C_{TDA}(g)$ count for a demographic group g associated with a given block group, MCD or place, we say that the $C_{TDA}(g)$ count (or ratio) provides a **reliable characteristic** for the block group, MCD, or place.



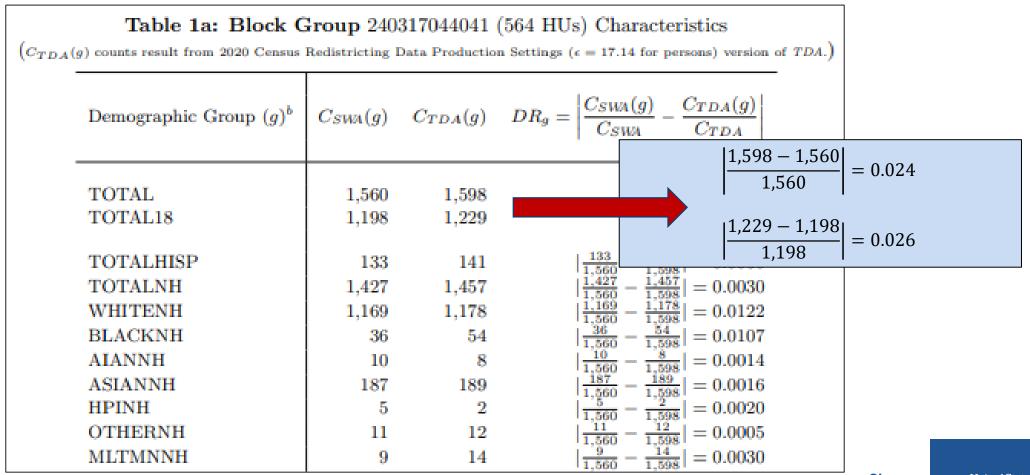
Part 1: Reliability of demographic characteristics

Table 1a: Block Group 240317044041 (564 HUs) Characteristics

 $(C_{TDA}(g) \text{ counts result from 2020 Census Redistricting Data Production Settings } (\epsilon = 17.14 \text{ for persons}) \text{ version of } TDA.)$

Demographic Group $(g)^b$	$C_{SWA}(g)$	$C_{TDA}(g)$	$DR_g = \left \frac{C_{SWA}(g)}{C_{SWA}} - \frac{C_{TDA}(g)}{C_{TDA}} \right $
TOTAL	1,560	1,598	c
TOTAL18	1,198	1,229	c
TOTALHISP	133	141	$\left \frac{133}{1,560} - \frac{141}{1,598}\right = 0.0030$
TOTALNH	1,427	1,457	$\left \frac{1,427}{1,560} - \frac{1,457}{1,598}\right = 0.0030$
WHITENH	1,169	1,178	$\left \frac{1,169}{1,560} - \frac{1,178}{1,598}\right = 0.0122$
BLACKNH	36	54	$\left \frac{36}{1,560} - \frac{54}{1,598}\right = 0.0107$
AIANNH	10	8	$\left \frac{10}{1,560} - \frac{8}{1,598}\right = 0.0014$
ASIANNH	187	189	$\left \frac{\frac{187}{1,560} - \frac{189}{1,598} \right = 0.0016}{\frac{5}{100000000000000000000000000000000000$
HPINH	5	2	$\left \frac{\frac{1,500}{5}}{\frac{1,560}{1,598}}\right = 0.0020$
OTHERNH	11	12	$\begin{vmatrix} \frac{10}{1,560} - \frac{8}{1,598} = 0.0014 \\ \frac{187}{1,560} - \frac{189}{1,598} = 0.0016 \\ \frac{5}{1,560} - \frac{2}{1,598} = 0.0020 \\ \frac{11}{1,560} - \frac{12}{1,598} = 0.0005 \\ \frac{9}{1,560} - \frac{14}{1,598} = 0.0030 \end{vmatrix}$
MLTMNNH	9	14	$\left \frac{\frac{9}{1,560}}{\frac{1}{1,598}}\right = 0.0030$

Part 1: Reliability of demographic characteristics



Shape your future START HERE >



Table 3: Proportion of Block Groups in Each Stratum for Three Criteria

(Proportion computations result from 2020 Census Redistricting Data Production Settings ($\epsilon = 17.14$ for persons) version of TDA.)

Population: United States (50 States & DC)

_							
			Reliable Characteristics Criteria				
	Stratum for Block Groups Using C_{SWA}	Number of Block	Criterion I	Criterion II	Criterion III		
	for TOTAL	Groups	LDG $DR_g \le 0.01$	LDG $DR_g \le 0.03$	LDG $DR_g \le 0.05$		
	$50 \le C_{SWA} \le 99$	128	0.1250	0.3594	0.5156		
	$100 \le C_{SW\!A} \le 149$	99	0.1818	0.5253	0.7071		
	$150 \le C_{SWA} \le 199$	124	0.1694	0.5565	0.7581		
	$200 \le C_{SWA} \le 249$	154	0.2662	0.6234	0.7922		
	$250 \le C_{SWA} \le 299$	209	0.2919	0.6459	0.8565		
	$300 \le C_{SWA} \le 349$	264	0.3636	0.7348	0.8902		
	$350 \le C_{SWA} \le 399$	407	0.3366	0.7346	0.8698		
	$400 \le C_{SWA} \le 449$	569	0.4077	0.7750	0.9315		
7	$450 \le C_{SWA} \le 499$	915	0.4087	0.8284	0.9552		
	$500 \le C_{SWA} \le 549$	1,699	0.4197	0.8458	0.9588		
	$550 \le C_{SWA} \le 599$	3,238	0.4546	0.8684	0.9654		
	$600 \le C_{SWA} \le 649$	5,131	0.4578	0.8827	0.9751		
	$650 \le C_{SWA} \le 699$	6,683	0.4718	0.8927	0.9753		
	$700 \le C_{SWA} \le 749$	$7,\!356$	0.5007	0.9082	0.9826		

Table 3
(continued)

$950 \le C_{SWA} \le 999$	8,723	0.5849	0.9512	0.9952
$1,000 \le C_{SWA} \le 1,049$	8,398	0.6044	0.9582	0.9952
$1,050 \le C_{SWA} \le 1,099$	8,345	0.6192	0.9646	0.9965
$1,100 \le C_{SWA} \le 1,149$	7,950	0.6244	0.9701	0.9972
$1,150 \le C_{SWA} \le 1,199$	7,860	0.6422	0.9763	0.9977
$1,200 \le C_{SWA} \le 1,249$	7,451	0.6515	0.9757	0.9988
$1,250 \le C_{SWA} \le 1,299$	7,124	0.6645	0.9749	0.9978
$1,300 \le C_{SWA} \le 1,349$	6,714	0.6822	0.9812	0.9988
$1,350 \le C_{SWA} \le 1,399$	6,507	0.6859	0.9866	0.9989
$1,400 \le C_{SWA} \le 1,449$	5,911	0.7090	0.9866	0.9992
$1,450 \le C_{SWA} \le 1,499$	5,617	0.7002	0.9858	0.9995
$1,500 \le C_{SWA} \le 1,549$	5,390	0.7330	0.9900	0.9994
$1,550 \le C_{SWA} \le 1,599$	4,856	0.7341	0.9866	0.9994
$1,600 \le C_{SWA} \le 1,649$	4,508	0.7420	0.9918	0.9998
$1,650 \le C_{SWA} \le 1,699$	4,325	0.7489	0.9908	0.9998
$1,700 \le C_{SWA} \le 1,749$	4,093	0.7669	0.9922	1.0000
$1,750 \le C_{SWA} \le 1,799$	3,689	0.7650	0.9938	0.9997
$1,800 \le C_{SWA} \le 1,849$	3,469	0.7530	0.9925	1.0000
$1,850 \le C_{SWA} \le 1,899$	3,252	0.7811	0.9945	0.9997
$1,900 \le C_{SWA} \le 1,949$	3,008	0.7793	0.9947	1.0000
$1,950 \le C_{SWA} \le 1,999$	2,832	0.7970	0.9965	1.0000
$2,000 \le C_{SWA} \le 2,049$	2,573	0.8022	0.9965	1.0000
$2,050 \le C_{SW\!A} \le 2,099$	2,356	0.7975	0.9966	1.0000
$2,100 \le C_{SWA} \le 2,149$	2,307	0.8331	0.9957	1.0000
$2,150 \le C_{SWA} \le 2,199$	2,033	0.8170	0.9975	1.0000
$2,200 \le C_{SWA} \le 2,249$	1,999	0.8354	0.9990	1.0000
$2,250 \le C_{SWA} \le 2,299$	1,892	0.8494	0.9984	1.0000
2200 / 0 - / 2240	1 000	A 0221	0.0000	1 0000

Table 3a: For Each Run, the Stratum and Stratum Proportion When 0.9500 First Exceeded

(Proportion computations result from 2020 Census Redistricting Data Production Settings (ε = 17.14 for persons) version of TDA.) Population: United States (50 States & DC)

		Criterion III LDG $DR_g \leq 0.05$
TDA Run	Stratum for Block Groups	Proportion When 0.9500 First Exceeded
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23	$\begin{array}{c} 450 \leq C_{SWA} \leq 499 \\ 400 \leq C_{SWA} \leq 449 \\ 400 \leq C_{SWA} \leq 449 \\ 350 \leq C_{SWA} \leq 399 \\ 450 \leq C_{SWA} \leq 499 \\ 450 \leq C_{SWA} \leq 499 \\ 400 \leq C_{SWA} \leq 449 \\ 450 \leq C_{SWA} \leq 499 \\ 350 \leq C_{SWA} \leq 399 \\ 450 \leq C_{SWA} \leq 499 \\ 350 \leq C_{SWA} \leq 499 \\ 350 \leq C_{SWA} \leq 399 \\ 450 \leq C_{SWA} \leq 399 \\ 450 \leq C_{SWA} \leq 399 \\ 350 \leq C_{SWA} \leq 399 \\ \end{array}$	0.9716 0.9596 0.9661 0.9543 0.9561 0.9508 0.9509 0.9541 0.9617 0.9661 0.9596 0.9683 0.9525 0.9543 0.9525 0.9543 0.9558 0.9607 0.9607 0.9607 0.9596 0.9727 0.9582 0.9617 0.9683 0.9558
24 25	$450 \le C_{SWA} \le 499$ $450 \le C_{SWA} \le 499$	0.9628 0.9519

Table 4: Proportion of Places and MCDs in Each Stratum for Three Criteria

(Proportion computations result from 2020 Census Redistricting Data Production Settings (ε = 17.14 for persons) version of TDA.)

Population: United States (50 States & DC)

-									
			Relial	Reliable Characteristics Criteria					
	Stratum for Places and MCDs Using C _{SWA} for TOTAL	Number of Places and MCDs	Criterion I LDG $DR_g \leq 0.01$	Criterion II ${\rm LDG}\ DR_g \leq 0.03$	Criterion III LDG $DR_g \leq 0.05$				
_	$50 \le C_{SW\!A} \le 99$	573	0.2182	0.5969	0.7923				
1	$100 \le C_{SWA} \le 149$ $150 \le C_{SWA} \le 199$	622 645	0.4051 0.3442	0.7540 0.8109	0.9116 0.9473				
7	$200 \le C_{SWA} \le 249$ $250 \le C_{SWA} \le 299$	598 500	0.4197 0.4860	0.8361 0.9000	0.9632				
	$300 \le C_{SWA} \le 299$ $300 \le C_{SWA} \le 349$	448	0.5379	0.9152	0.9760 0.9844				
	$350 \le C_{SWA} \le 399$ $400 \le C_{SWA} \le 449$	417 399	0.5731 0.6416	0.9233 0.9449	0.9808 0.9975				
	$450 \le C_{SWA} \le 499$	344	0.6424	0.9680	0.9913				
	$500 \le C_{SWA} \le 549$ $550 \le C_{SWA} \le 599$	341 291	0.6716 0.7113	0.9765 0.9691	0.9971 0.9966				



Table 4 (continued)

$850 \le C_{SWA} \le 899$	222	0.7162	0.9955	1.0000
$900 \le C_{SWA} \le 949$	201	0.7562	0.9851	1.0000
$950 \le C_{SWA} \le 999$	210	0.7571	0.9952	1.0000
$1,000 \le C_{SWA} \le 1,049$	223	0.7982	0.9955	1.0000
$1,050 \le C_{SWA} \le 1,099$	157	0.8153	0.9873	1.0000
$1,100 \le C_{SWA} \le 1,149$	194	0.7423	0.9897	0.9948
$1,150 \le C_{SWA} \le 1,199$	178	0.8596	1.0000	1.0000
$1,200 \le C_{SWA} \le 1,249$	162	0.8395	1.0000	1.0000
$1,250 \le C_{SWA} \le 1,299$	174	0.8563	0.9885	1.0000
$1,300 \le C_{SWA} \le 1,349$	164	0.8659	0.9939	1.0000
$1,350 \le C_{SWA} \le 1,399$	166	0.8614	1.0000	1.0000
$1,400 \le C_{SWA} \le 1,449$	134	0.9030	0.9851	0.9925
$1,450 \le C_{SWA} \le 1,499$	153	0.8562	0.9935	1.0000
$1.500 \le C_{Swa} \le 1.549$	147	0.9320	1.0000	1.0000

Table 4a: For Each Run, the Stratum and Stratum Proportion When 0.9500 First Exceeded

(Proportion computations result from 2020 Census Redistricting Data Production Settings (ε = 17.14 for persons) version of TDA.) Population: United States (50 States & DC)

		Criterion III LDG $DR_g \le 0.05$
TDA Run	Stratum for Places & MCDs	Proportion When 0.9500 First Exceeded
1	$150 \le C_{SWA} \le 199$	0.9504
2	$200 \le C_{SWA} \le 249$	0.9548
3	$150 \le C_{SWA} \le 199$	0.9566
4	$150 \le C_{SWA} \le 199$	0.9504
5	$200 \le C_{SWA} \le 249$	0.9632
6	$200 \le C_{SWA} \le 249$	0.9632
7	$200 \le C_{SWA} \le 249$	0.9615
8	$200 \le C_{SWA} \le 249$	0.9615
9	$200 \le C_{SWA} \le 249$	0.9582
10	$150 \le C_{SWA} \le 199$	0.9643
11	$150 \le C_{SWA} \le 199$	0.9566
12	$150 \le C_{SWA} \le 199$	0.9504
13	$200 \le C_{SWA} \le 249$	0.9615
14	$150 \le C_{SWA} \le 199$	0.9550
15	$200 \le C_{SWA} \le 249$	0.9565
16	$150 \le C_{SWA} \le 199$	0.9550
17	$200 \le C_{SWA} \le 249$	0.9515
18	$150 \le C_{SWA} \le 199$	0.9519
19	$150 \le C_{SWA} \le 199$	0.9504
20	$200 \le C_{SWA} \le 249$	0.9532
21	$200 \le C_{SWA} \le 249$	0.9615
22	$200 \le C_{SWA} \le 249$	0.9548
23	$150 \le C_{SWA} \le 199$	0.9566
24	$150 \le C_{SWA} \le 199$	0.9550
25	$150 \le C_{SWA} \le 199$	0.9519

Analysis of Congressional and State Legislative Districts

Another type of defined geography that is not a part of this nesting includes Congressional districts and state legislative districts. As we will see with Rhode Island in Part II of this study report, each state has Congressional district(s) (CD), state legislative districts in an upper chamber (SLDU), and state legislative districts in a lower chamber (SLDL).

As with the summary display in Table 3a for block groups and the summary display in Table 4a for places and MCDs, we use results from the 25 runs for all "Congressional and state legislative districts". Altogether, we make use of all 7,167 (= 436 + 1,946 + 4,785) Congressional and state legislative districts in the United States. The Table below gives a few parameters for the national accounting of these districts.

	CD	SLDU	SLDL
Number of Districts	436	1,946	4,785
Min Population	526,283	13,629	3,173
Median Population	705,831	121,212	41,713
Mean Population	708,132	158,656	64,016
Max Population	989,415	940,612	470,325

Table 5: For Each Run, the Stratum and Stratum Proportion When 0.9500 First Exceeded

(Proportion computations result from 2020 Census Redistricting Data Production Settings (\$\epsilon = 17.14\$ for persons) version of TDA.)

Population: United States (50 States & DC)

		Criterion III LDG $DR_g \leq 0.05$
TDA Run	Stratum for Congressional & State Legislative Districts	Proportion When 0.9500 First Exceeded
1	$3,150 \le C_{SW3} \le 3,199$	1.0000
2	$3,150 \le C_{SWA} \le 3,199$	1.0000
3	$3,150 \le C_{SWA} \le 3,199$	1.0000
4	$3,150 \le C_{SWA} \le 3,199$	1.0000
5	$3,150 \le C_{SWA} \le 3,199$	1.0000
6	$3,150 \le C_{SWA} \le 3,199$	1.0000
7	$3,150 \le C_{SWA} \le 3,199$	1.0000
8	$3,150 \le C_{SWA} \le 3,199$	1.0000
9	$3,150 \le C_{SWA} \le 3,199$	1.0000
10	$3,150 \le C_{SWA} \le 3,199$	1.0000
11	$3,150 \le C_{SWA} \le 3,199$	1.0000
12	$3,150 \le C_{SWA} \le 3,199$	1.0000
13	$3,150 \le C_{SWA} \le 3,199$	1.0000
14	$3,150 \le C_{SWA} \le 3,199$	1.0000
15	$3,150 \le C_{SWA} \le 3,199$	1.0000
16	$3,150 \le C_{SWA} \le 3,199$	1.0000
17	$3,150 \le C_{SWA} \le 3,199$	1.0000
18	$3,150 \le C_{SWA} \le 3,199$	1.0000
19	$3,150 \le C_{SWA} \le 3,199$	1.0000
20	$3,150 \le C_{SWA} \le 3,199$	1.0000
21	$3,150 \le C_{SWA} \le 3,199$	1.0000
22	$3,150 \le C_{SWA} \le 3,199$	1.0000
23	$3,150 \le C_{SWA} \le 3,199$	1.0000
24	$3,150 \le C_{SWA} \le 3,199$	1.0000
25	$3,150 \le C_{SWA} \le 3,199$	1.0000

Wright and Irimata (2021) Part 2: Variability across DAS runs

Part 2 of their analysis examines 25 independent runs of 2010 Census data through the 2020 Census DAS using the same production settings to assess variability across runs.

The resulting data were then assessed for their variability against a range of redistricting use cases:

- Rhode Island's Congressional Districts (2)
- Rhode Island's State Upper Legislative Districts (38)
- Rhode Island's State Lower Legislative Districts (75)
- DOJ-supplied jurisdictions
 - Panola County, Mississippi (2,180 blocks)
 - Tate County (School District), Mississippi (784 blocks)
 - Tylertown (Walthall County), Mississippi (136 blocks)





Wright and Irimata (2021) Part 2: Variability across DAS runs

Definitions of Redistricting Measures of Variation. The measures defined here are all for a specific ε. Henceforth, and to simplify notation, we use S for SWA and T for TDA. Let

≡ the number of demographic groups;

 $C_S(q) \equiv$ the population of group q (2010 Census, SF1), for q = 1, ..., G; and

 \equiv the population of group q resulting from the ith TDA run, for i = 1, ..., 25,

We have the following measures including two types of variation among the 25 TDA runs within group g: one relative to $\bar{C}_T(g)$ (see below) and another relative to $C_S(g)$.

The average population of group q over the 25 TDA runs is

$$\bar{C}_T(g) \equiv \frac{C_{T1}(g) + C_{T2}(g) + \dots + C_{T,25}(g)}{25}.$$

The variation(1) among the population of group q over the 25 TDA runs is

$$V(1)_g \equiv \frac{[C_{T1}(g) - \bar{C}_T(g)]^2 + [C_{T2}(g) - \bar{C}_T(g)]^2 + \dots + [C_{T,25}(g) - \bar{C}_T(g)]^2}{25}.$$

The relative variation(1) among the population of group q over the 25 TDA runs is

$$RV(1)_g \equiv \frac{\sqrt{V(1)_g}}{\bar{C}_T(g)}$$
.

The average relative variation (1) among the population over the G groups (essentially a coefficient of variation) is

$$AV\!ERV(1) \equiv \frac{RV(1)_1 + RV(1)_2 + \cdots + RV(1)_G}{G}.$$

Part 2: Variability across DAS runs

Figure 1

Jurisdiction	District	IDEAL POPULATION	AVERV(1)
Rhode Island	CD-01	526,283.50	0.006
Rhode Island	CD-02	526,283.50	0.008
Rhode Island	SLDU-01	27,699.10	0.036
Rhode Island	SLDU-02	27,699.10	0.051
Rhode Island	SLDU-03	27,699.10	0.045
Rhode Island	SLDU-04	27,699.10	0.048
Rhode Island	SLDL-01	14,034.20	0.067
Rhode Island	SLDL-02	14,034.20	0.069
Rhode Island	SLDL-03	14,034.20	0.057
Rhode Island	SLDL-04	14,034.20	0.104
Panola County, MS	D-01	6,941.40	0.362
Panola County, MS	D-02	6,941.40	0.353
Panola County, MS	D-03	6,941.40	0.344
Panola County, MS	D-04	6,941.40	0.369
Panola County, MS	D-05	6,941.40	0.280
Tate County Schools, MS	D-01	3,764.60	0.335
Tate County Schools, MS	D-02	3,764.60	0.355
Tate County Schools, MS	D-03	3,764.60	0.493
Tate County Schools, MS	D-04	3,764.60	0.449
Tate County Schools, MS	D-05	3,764.60	0.376
Tylertown, MS	D-01	402.25	0.748
Tylertown, MS	D-02	402.25	0.622
Tylertown, MS	D-03	402.25	0.596
Tylertown, MS	D-04	402.25	1.265



Wright and Irimata (2021) Conclusions

The Key Empirical Message on Reliability:

"for any block group with a TOTAL count between 450 and 499 people or larger, and for MCDs and places between 200 and 249 or larger, the difference between the TDA ratio of the largest demographic group (LDG) and the corresponding SWA ratio for the LDG is less than or equal to 5 percentage points at least 95% of the time". No Congressional or state legislative district fails this test; that is, for these districts, the 5-percentage point criterion holds 100% of the time."

The Key Empirical Message on Variability:

"relative variability in the TDA [decreases] as we consider [larger] pieces of geography and population...At a high level, [the analysis] tends to show less relative variability using the 2020 Census redistricting data production settings version of the TDA than the 2021-04-28 version



Analysis of the impact of DAS production settings on the identification of majority-minority districts





Districts Examined:

Congressional Districts	436
State Upper Legislative Districts (SLDU)	1,946
State Lower Legislative Districts (SLDL)	4,785



Demographics Examined:

P1/P8 Tables (Total Population by Race):

- White Alone
- Black Alone
- AIAN Alone
- Asian Alone
- SOR Alone
- Black and Black+White

P2/P9 Tables (Total Hispanic/NH by Race):

- Hispanic
- NH White Alone
- NH Black Alone
- NH AIAN Alone
- NH Asian Alone
- NH SOR Alone
- NH Black and Black+White

NH = Not Hispanic

P3/P10 Tables (VAP by Race):

- White Alone VAP
- Black Alone VAP
- AIAN Alone VAP
- Asian Alone VAP
- SOR Alone VAP
- Black and Black+White VAP

P4/P11 Tables (Hispanic/NH VAP by Race):

- Hispanic VAP
- NH White Alone VAP
- NH Black Alone VAP
- NH AIAN Alone VAP
- NH Asian Alone VAP
- NH SOR Alone VAP
- NH Black and Black+White VAP

VAP = Voting Age Population



P1/P8 Tables (Total Population by Race)

White Alone

State	District	District Type	SF1 Total		SF1 White	DAS White	SF1 %White	DAS %White
27	062	Upper	79,225	79,289	39,665	39,639	50.01%	49.99%
6	46	Cong.	702,906	702,803	351,403	351,441	49.99%	50.01%

Black Alone

State		District Type	SF1 Total		SF1 Black		SF1 %Black	DAS %Black
1	085	Lower	45,229	45,206	22,651	22,581	50.08%	49.95%



P2/P9 Tables (Total Hispanic)

Total Hispanic:

State		District Type		DAS Total	_	_		DAS %Hispanic
32	014	Lower	64,054	63,906	31,975	31,964	49.92%	50.02%



P2/P9 Tables (Total NH by Race)

NH White Alone:

State	District	District Type	SF1 Total	DAS Total	SF1 NH White	DAS NH White	SF1 %NH White	DAS %NH White
51	050	Lower	80,677	80,712	40,353	40,353	50.02%	50.00%*
32	009	Upper	128,882	128,641	64,380	64,343	49.95%	50.02%

NH Black Alone:

State		District Type		_			SF1 %NH Black	DAS %NH Black
37	043	Lower	79,233	79,025	39,545	39,551	49.91%	50.05%

NH AIAN Alone:

State		District Type			SF1 NH AIAN		SF1 %NH AIAN	DAS %NH AIAN
30	015	Lower	9,595	9,610	4,807	4,744	50.10%	49.37%

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P3/P10 Tables (Voting Age by Race)

VAP White Alone:

State		District Type		DAS Total		DAS VAP White	SF1 %VAP White	DAS %VAP White
27	40A	Lower	27,864	27,904	13,934	13,938	50.01%	49.95%

VAP Black Alone:

State		District Type	SF1 Total	_	SF1 VAP Black	DAS VAP Black	SF1 %VAP Black	DAS %VAP Black
26	005	Upper	196,028	196,209	98,101	98,071	50.04%	49.98%
37	058	Lower	61,968	61,983	30,954	31,003	49.95%	50.02%

VAP Black and Black+White:

State	District	District Type	SF1 Total	DAS Total	SF1 VAP Black	DAS VAP Black	SF1 %VAP Black	DAS %VAP Black
37	057	Lower	59,215	59,273	29,589	29,660	49.97%	50.04%
37	12	Cong.	544,436	544,179	272,110	272,256	49.98%	50.03%

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P4/P11 Tables (Hispanic VAP)

Hispanic VAP:

State	District	District Type	SF1 Total	DAS Total	SF1 VAP Hisp.	DAS VAP Hisp.	SF1 %VAP Hisp.	DAS %VAP Hisp.
12	014	Upper	342,997	342,819	171,560	171,389	50.02%	49.99%
12	087	Lower	115,237	115,148	57,642	57,538	50.02%	49.97%



P4/P11 Tables (Not Hispanic VAP by Race)

VAP NH White:

State	District	District Type	SF1 Total	DAS Total	VAP NH	DAS VAP NH White		DAS %VAP NH White
27	062	Upper	60,648	60,720	30,384	30,359	50.10%	50.00%*

VAP NH Black Alone:

State	District	District Type	SF1 Total	DAS Total	SF1 VAP NH Black	DAS VAP NH Black	SF1 %VAP NH Black	DAS %VAP NH Black
13	177	Lower	41,506	41,461	20,719	20,731	49.92%	50.00%
18	094	Lower	45,634	45,508	22,786	22,837	49.93%	50.18%
26	001	Upper	197,305	196,969	98,476	98,500	49.91%	50.01%
42	181	Lower	45,240	45,073	22,614	22,644	49.99%	50.24%

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P4/P11 Tables (Not Hispanic VAP by Race)

VAP NH Black and Black+White:

State	District	District Type	SF1 Total	DAS Total	SF1 VAP NH Black	DAS VAP NH Black	SF1 %VAP NH Black	DAS %VAP NH Black
9	015	Lower	18,820	18,863	9,422	9,423	50.06%	49.95%
45	023	Lower	28,442	28,433	14,230	14,202	50.03%	49.95%
24	37A	Lower	30,391	30,391	15,118	15,199	49.74%	50.01%
36	05	Cong.	545,319	545,308	272,480	272,949	49.97%	50.05%
37	043	Lower	59,130	59,881	29,480	29,446	49.86%	50.01%

Conclusions

Comparison of the Production Settings Demonstration Data to the published 2010 Census tabulations identified 25 districts out of 7,167 (0.3%) where a demographic group *could* be considered to flip from majority to minority or vice-versa.

Flips occurred in both directions (11 groups went from majority to minority, 14 went from minority to majority).

No flips involved both a racial or ethnic group's total population and voting age population. (That is, districts drawn to have majorities of both total population and voting age population are more stable.)

All flips involved very small numbers of individuals in districts that were tightly drawn (usually within a few hundredths of a percent of the 50% mark) using the published 2010 Census tabulations (a level of precision that would be greatly impacted by the noise injected by the 2010 Census swapping algorithms).





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